#### Improved Fusion of Visual and Language Representations by Dense Symmetric Co-Attention for Visual Question Answering

#### Duy-Kien Nguyen, Takayuki Okatani

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Reading group

Presented by: Sebastian Bujwid

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  - Model: *dense co-attention network* (DCN)
- State-of-the-art results on VQA and VQA 2.0 datasets

## Background

## Soft attention mechanism

- $q \in \mathbb{R}^{d_q}$  query
- $K \in \mathbb{R}^{L imes d_k}$  keys
- $V \in \mathbb{R}^{L imes d_v}$  values

$$egin{aligned} & [lpha_1,\ldots,lpha_L] = ext{softmax}(f(q,K)) \ & ext{attention}(q,K,V) = \sum_{i=1}^L lpha_i v_i \end{aligned}$$

• 
$$v_i \in V$$

•  $f: \mathbb{R}^{d_q} imes \mathbb{R}^{L imes d_k} o \mathbb{R}^L$  - compatibility function









## Why attention mechanism?

- Conditional representations
- Meaning of a word in the context of a sentence
- Meaning of an object in the context of a question





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- O(1) vs. O(N) for RNNs





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- Conditional representations
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- Meaning of an object in the context of a question
- Modeling long-term dependencies
- $\circ O(1)$  vs. O(N) for RNNs
- Some interpretability

### Attention mechanism - VQA



What are these animals

What are these animals

Is it cloudy

Pred: Giraffes, Ans: Giraffes



Is it cloudy Pred: No, Ans: No

• Focus at relevant regions or relevant question words

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- Representations conditioned on the context



What sport is this woman playing

## Dot-product attention

- $q \in \mathbb{R}^{d_q}$  query
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#### $\operatorname{attention}(Q,K,V) = \operatorname{softmax}(QK^\top)V$

•  $d_q = d_k$ 

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## Method: DCN

dense, bi-directional interactions between the two modalities

- Each word represented in the context of the image
- Each image region represented in the context of the question

## DCN - attention maps

- +  $Q_l = [q_{l1}, \dots, q_{lN}] \in \mathbb{R}^{d imes N}$  N question words
- $V_l = [v_{l1}, \dots, v_{lT}] \in \mathbb{R}^{d imes T}$  T image regions

Compute the affinity matrix:

$$A_l = V_l^ op W_l Q_l$$

•  $A_l \in \mathbb{R}^{T imes N}$ 

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$$egin{aligned} A_{Q_l} &= ext{softmax}(A_l) \ A_{V_l} &= ext{softmax}ig(A_l^{ op}ig) \end{aligned}$$

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This is of course **not** exactly what they do!

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• Multiple attention maps:  $oldsymbol{A}_l^{(i)}$  instead of  $oldsymbol{A}_l$ , where  $oldsymbol{i}$  - attention number

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$$W_{ ilde{V}_l}^{(i)} \in \mathbb{R}^{d_h imes d}$$
,  $W_{ ilde{Q}_l}^{(i)} \in \mathbb{R}^{d_h imes d}$ 

$$A_l^{(i)} = \left( W_{ ilde{V}_l}^{(i)} ilde{V}_l 
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• Alternative low-rank approach:

Kim, Jin-Hwa, Jaehyun Jun, and Byoung-Tak Zhang. "Bilinear attention networks." *Advances in Neural Information Processing Systems*. 2018.

Scaled by  $\sqrt{d_h}$  (not justified in the paper)

$$A_{Q_l}^{(i)} = ext{softmax}igg(rac{A_l^{(i)}}{\sqrt{d_h}}igg)$$

$$A_{V_l}^{(i)} = ext{softmax}igg(rac{A_l^{(i) op}}{\sqrt{d_h}}igg)$$

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- For high  $d_h$  the variance of dot products is high very small gradients
- The scaling results in smoother distribution

$$egin{aligned} A_{Q_l} &= rac{1}{h} \sum_{i=1}^h A_{Q_l}^{(i)} \ A_{V_l} &= rac{1}{h} \sum_{i=1}^h A_{V_l}^{(i)} \end{aligned}$$

- \$\$A\_{Q\_l} \in \mathbb{R}^{\tilde{T} \times \tilde{N}}\$\$ word probability for each image region
  \$\$A\_{V\_l} \in \mathbb{R}^{\tilde{N} \times \tilde{T}}\$\$ image region probability for each word

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#### Attended feature representations:

$$\hat{Q}_l = ilde{Q}_l A_{Q_l} [1:\mathrm{T},:]^ op$$

-  $\hat{Q}_l \in \mathbb{R}^{d imes T}$  - an average of word vectors weighted by their relevance to (compatibility with) the image regions

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$$\hat{V_l} = ilde{V_l} A_{V_l} [1:\mathrm{N},:]^ op$$

-  $\hat{V_l} \in \mathbb{R}^{d \times N}$  - an average of image region vectors weighted by their relevance to (compatibility with) the word

These are **still unimodal representations**, just attended

## Fusing representations

Each word is fused with a (**unique**) representation of the image

$$q_{(l+1)n} = ext{ReLU}igg(W_{Q_l}igg[ egin{matrix} q_{ln} \ \hat{v}_{ln} \end{bmatrix} + b_{Q_l}igg) + q_{ln}$$

-  $\hat{v}_{ln}$  - meaning of the image in the context of the *n*-th word

Each image region is fused with a (**unique**) representation of the question

$$v_{(l+1)t} = ext{ReLU}igg(W_{V_l}igg[ egin{smallmatrix} v_{lt}\ \hat{q}_{\,lt} \end{bmatrix} + b_{V_i}igg) + v_{lt}$$

•  $\hat{q}_{lt}$  - meaning of the question in the context of the *t*-th image region

### DCN model



Figure 3: Computation of dense co-attention maps and attended representations of the image and question.



Figure 2: The internal structure of a single dense coattention layer of layer index l + 1.

## DCN model



Figure 1: The global structure of the dense co-attention network (DCN).

### Question representation

$$\overrightarrow{q_n} = ext{Bi-LSTM}\left( \overrightarrow{q_{n-1}}, e_n^Q 
ight)$$
 $\overleftarrow{q_n} = ext{Bi-LSTM}\left( \overleftarrow{q_{n+1}}, e_n^Q 
ight)$ 

•  $e_n^Q$  - GloVe embedding of the *n*-th word

$$q_n = \left[ \overrightarrow{q_n}^ op, \overleftarrow{q_n}^ op 
ight]^ op$$

$$Q = [q_1, \dots, q_N] \in \mathbb{R}^{d imes N}$$

### Image representation

4 layers from ResNet-152

- Each layer of different depth
- Different shapes  $\rightarrow$  max pooling and 1 x 1 convolution  $\rightarrow$  4 layers, each of shape  $d \times 14 \times 14$

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The relative importance of features corresponding to each depth level depends on the given question:

 $\left[lpha_{1},lpha_{2},lpha_{3},lpha_{4}
ight]= ext{softmax}( ext{MLP}\left(s_{Q}
ight))$ 

- Features weighted by alphas are summed together
- $V = [v_1, \dots, v_T] \in \mathbb{R}^{d imes T}$
- $T = 14 \times 14$

### DCN - predicting answers

$$egin{aligned} s_{Q_L} &= \sum_{n=1}^N lpha_n^Q q_{Ln} \ s_{V_L} &= \sum^N lpha_n^V v_{Ln} \end{aligned}$$

n=1

Different methods for predicting answers:

$$egin{aligned} & ( ext{score of answers encoded as } s_A) = \sigma \left( s_A^ op W \left( s_{Q_L} + s_{V_L} 
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ight), ( extsf{16}) \ & ( ext{ score of answers }) = \sigma \left( ext{MLP} ig( s_{Q_L} + s_{V_L} ig) ig), ( extsf{17}) \ & ( ext{ score of answers }) = \sigma \left( ext{MLP} ig( igst| igst| s_{Q_L} igst| igst) igst), ( extsf{18}) \end{aligned}$$

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• (17) and (18) can produce only answers that are considered when training

## Experiments

## Datasets

• Images from MS-COCO (200k+ images)

VQA (1.0):

• 240k+ train, 120k+ val, 240k+ test questions

VQA 2.0:

- The largest VQA dataset
- 440k+ train, 210k+ val, 440k+ test questions
- Reduced language bias



### Results VQA 1.0

Table 2: Results of the proposed method along with published results of others on VQA 1.0 in similar conditions (i.e., a single model; trained without an external dataset).

| Model                | Test-dev |       |        |        | Test-standard |       |        |        |
|----------------------|----------|-------|--------|--------|---------------|-------|--------|--------|
|                      | Overall  | Other | Number | Yes/No | Overall       | Other | Number | Yes/No |
| VQA team [2]         | 57.75    | 43.08 | 36.77  | 80.50  | 58.16         | 43.73 | 36.53  | 80.569 |
| SMem [31]            | 57.99    | 43.12 | 37.32  | 80.87  | 58.24         | 43.48 | 37.53  | 80.80  |
| SAN [32]             | 58.70    | 46.10 | 36.60  | 79.30  | 58.90         | -     | -      | -      |
| FDA [12]             | 59.24    | 45.77 | 36.16  | 81.14  | 59.54         | -     | -      | -      |
| DNMN [1]             | 59.40    | 45.50 | 38.60  | 81.10  | 59.40         | -     | -      | -      |
| HieCoAtt [21]        | 61.00    | 51.70 | 38.70  | 79.70  | 62.10         | -     | -      | -      |
| RAU [24]             | 63.30    | 53.00 | 39.00  | 81.90  | 63.20         | 52.80 | 38.20  | 81.70  |
| DAN [23]             | 64.30    | 53.90 | 39.10  | 83.00  | 64.20         | 54.00 | 38.10  | 82.80  |
| Strong Baseline [14] | 64.50    | 55.20 | 39.10  | 82.20  | 64.60         | 55.20 | 39.10  | 82.00  |
| MCB [6]              | 64.70    | 55.60 | 37.60  | 82.50  | -             | -     | -      | -      |
| N2NMNs [11]          | 64.90    | -     | -      | -      | -             | -     | -      | -      |
| MLAN [35]            | 64.60    | 53.70 | 40.20  | 83.80  | 64.80         | 53.70 | 40.90  | 83.70  |
| MLB [16]             | 65.08    | 54.87 | 38.21  | 84.14  | 65.07         | 54.77 | 37.90  | 84.02  |
| MFB [36]             | 65.90    | 56.20 | 39.80  | 84.00  | 65.80         | 56.30 | 38.90  | 83.80  |
| MF-SIG-T3 [5]        | 66.00    | 56.37 | 39.34  | 84.33  | 65.88         | 55.89 | 38.94  | 84.42  |
| DCN (16)             | 66.43    | 56.23 | 42.37  | 84.75  | 66.39         | 56.23 | 41.81  | 84.53  |
| DCN (17)             | 66.89    | 57.31 | 42.35  | 84.61  | 67.02         | 56.98 | 42.34  | 85.04  |
| DCN (18)             | 66.83    | 57.44 | 41.66  | 84.48  | 66.66         | 56.83 | 41.27  | 84.61  |

### Results VQA 2.0

Table 3: Results of the proposed method along with published results of others on VQA 2.0 in similar conditions (i.e., a single model; trained without an external dataset). DCN(number) indicates the DCN equipped with the prediction layer that uses equation (number) for score computation. \*: trained with external datasets. ‡: the winner of VQA challenge 2017, unpublished.

| Model                        | Test-dev |       |        | Test-standard |         |       |        |        |
|------------------------------|----------|-------|--------|---------------|---------|-------|--------|--------|
|                              | Overall  | Other | Number | Yes/No        | Overall | Other | Number | Yes/No |
| VQA team-Prior [8]           | -        | -     | -      | -             | 25.98   | 01.17 | 00.36  | 61.20  |
| VQA team-Language only [8]   | -        | -     | -      | -             | 44.26   | 27.37 | 31.55  | 67.01  |
| VQA team-LSTM+CNN [8]        | -        | -     | -      | -             | 54.22   | 41.83 | 35.18  | 73.46  |
| MCB [6] reported in [8]      | -        | -     | -      | -             | 62.27   | 53.36 | 38.28  | 78.82  |
| MF-SIG-T3 * [5]              | 64.73    | 55.55 | 42.99  | 81.29         | -       | -     | -      | -      |
| Adelaide Model * ‡ [28]      | 62.07    | 52.62 | 39.46  | 79.20         | 62.27   | 52.59 | 39.77  | 79.32  |
| Adelaide + Detector * ‡ [28] | 65.32    | 56.05 | 44.21  | 81.82         | 65.67   | 56.26 | 43.90  | 82.20  |
| DCN (16)                     | 66.87    | 57.26 | 46.61  | 83.51         | 66.97   | 57.09 | 46.98  | 83.59  |
| DCN (17)                     | 66.72    | 56.77 | 46.65  | 83.70         | 67.04   | 56.95 | 47.19  | 83.85  |
| DCN (18)                     | 66.60    | 56.72 | 46.60  | 83.50         | 67.00   | 56.90 | 46.93  | 83.89  |

## Ablation study

Table 1: Ablation study on each module of DCNs using the validation set of the Open-Ended task (VQA 2.0). \* indicates modules employed in the final model.

| Category            | Detail                                 | Accuracy |
|---------------------|--|----------|
| Attention direction | $\mathbf{I} \gets \mathbf{Q}$          | 60.95    |
|                     | $\mathrm{I} \to \mathrm{Q}$            | 62.63    |
|                     | $\mathrm{I}\leftrightarrow\mathrm{Q*}$ | 62.94    |
| Memory size $(K)$   | 1                                      | 62.53    |
|                     | 3*                                     | 62.94    |
|                     | 5                                      | 62.83    |
| Number $(h)$ of     | 2                                      | 62.82    |
| parallel attention  | 4*                                     | 62.94    |
| maps                | 8                                      | 62.81    |
| Number $(L)$ of     | 1                                      | 62.43    |
| stacked layers      | 2                                      | 62.82    |
|                     | 3*                                     | 62.94    |
|                     | 4                                      | 62.67    |
| Attention in answer | Attention used*                        | 62.94    |
| prediction layer    | Avg of features                        | 61.63    |
| Attention in image  | Attention used*                        | 62.94    |
| extraction layer    | Only last conv layer                   | 62.39    |

- $(I \leftarrow Q)$  question-guided attention on image region
- $(I \rightarrow Q)$  image-guided attention on question words
- $(I \leftrightarrow Q)$  DCN co-attention: attention in both directions

## How deep features?

- Layer 1:
  - *Yes/No* questions *is/are/does/can/could*
- Layer 3:
  - High importance on questions about colors
- Layer 4:
  - Highest importance in general
  - semantics: what



### Qualitative evaluation







Pred: Yellow, Ans: Yellow

Pred: White, Ans: White





What is the name of the utensil What is the name of the utensil Pred: Fork, Ans: Fork



What is the name of the utensil What is the name of the utensil Pred: Fork, Ans: Spoon (Error type: 1)



Pred: 5 feet, Ans: Tall (Error type: 1)

Pred: 5 feet, Ans: 6 feet (Error type: 2)





What is the color of pants the What is the color of pants the woman is wearing Pred: Plaid, Ans: Red and White (Error type: 4)



What is the color of pants the What is the color of pants the woman is wearing Pred: Green, Ans: Black (Error type: 4)



What color is lit up on the What color is lit up on the street lights Pred: Yellow, Ans: Green (Error type: 3)



What color is lit up on the What color is lit up on the street lights street lights Pred: White, Ans: None (Error type: 1)



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  - Permuation of the order of the features (but not the inputs) has no effect
  - Global or relative positions

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- Often high dataset biases in VQA problems
- Do attention maps look at the same regions as humans?
  - Das, Abhishek, et al. "Human attention in visual question answering: Do humans and deep networks look at the same regions?." *Computer Vision and Image Understanding 163 (2017): 90-100.*

## The End