2D1260, Finite Element Methods, HT03, Ninni Carlsund Levin, Exercise 3

Example 1

Calculate the integral

$$\int_{\Omega} x \ dxdy$$

where Ω is the polygon area with corners in (x, y) = (2, 1), (9, 2), (10, 4) and (6, 5).

Example 2

Given the nodal values $U_1 = u(2, 1)$, $U_2 = u(9, 2)$, $U_3 = u(10, 4)$ and $U_4 = u(6, 5)$. Give an approximation of the value u(7, 2).

Example 3

$$-\frac{d}{dx}\left(k\frac{du}{dx}\right) = f \quad \text{in } 2 < x < 4 \quad \text{with } u(2) = 0 \text{ and } u'(4) = 0$$

Solve the problem with k(x) = 1 and f(x) = 1 using 2 quadratic finite elements with endpoints in x = 2, x = 2.8 and x = 4.

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