## Datorarkitektur, 2008

## Tentamen 2008-03-14

## Instructions:

- Make sure that your exam is not missing any sheets, then write your full name on the front.
- Write your answers in the space provided below the problem. If you make a mess, clearly indicate your final answer.
- The exam has a maximum score of 60 points plus 3 possible bonus points.
- The aproximate limits for grades on this exam are:
- To pass (grade E): 30 points.
- For grade D: 37 points.
- For grade C: 45 points.
- For grade B: 52 points.
- For grade A: 59 points.
- The problems are of varying difficulty. The point value of each problem is indicated. Pile up the easy points quickly and then come back to the harder problems.
- This exam is OPEN BOOK. You may use any books or notes you like. Good luck!


## Problem 1. (8 points):

Consider a 7-bit two's complement representation. Fill in the empty boxes in the following table. Addition and subtraction should be performed based on the rules for 7-bit, two's complement arithmetic

| Number | Decimal Representation | Binary Representation |
| :---: | :---: | :---: |
| Zero | 0 |  |
| $\mathrm{n} / \mathrm{a}$ | -3 |  |
| $\mathrm{n} / \mathrm{a}$ | 11 |  |
| $\mathrm{n} / \mathrm{a}$ | -17 | 0110011 |
| $\mathrm{n} / \mathrm{a}$ |  | 10010 |
| $\mathrm{n} / \mathrm{a}$ |  |  |
| TMax |  |  |
| TMin |  |  |
| TMin+TMin |  |  |
| TMin+1 |  |  |
| TMax+1 |  |  |
| -TMax |  |  |
| -TMin |  |  |

## Problem 2. (8 points):

Consider the source code below, where M and N are constants declared with \#define.

```
int mat1[M][N];
int mat2[N][M];
int copy_element(int i, int j)
{
    mat1[i][j] = mat2[j][i];
}
```

This generates the following assembly code:

```
copy_element:
    pushl %ebp
    movl %esp, %ebp
    movl 12(%ebp), %edx
    leal 0(,%edx,8), %eax
    movl 8(%ebp), %ecx
    subl %edx, %eax
    pushl %ebx
    leal (%ecx,%eax,2), %eax
    leal (%ecx,%ecx,8), %ebx
    movl mat2(,%eax,4), %eax
    addl %edx, %ebx
    movl %eax, mat1(,%ebx,4)
    popl %ebx
    leave
    ret
```

A. What is the value of M :
B. What is the value of N :

## Problem 3. (14 points):

Consider the source code below, used to keep track of the rooms currently reserved in a family-run hotel. Each entry in the residents array stores a name of the customer reserving the room. FLOORS represents the number of floors in the hotel. ROOMS represents the number of rooms per floor. Both are constants declared with \#define. LEN, the maximum number of bytes allocated for a name, is defined to be 12 .

```
char residents[FLOORS][ROOMS][LEN];
void
reserve_room(int floor, int room, char *custname)
{
    strcpy(residents[floor][room], custname);
}
```

The assembly code for the function reserve_room looks like this:

```
reserve_room:
    pushl %ebp
    movl %esp,%ebp
    movl 12(%ebp),%eax
    movl 16(%ebp),%edx
    pushl %edx
    movl 8(%ebp),%edx
    sall $4,%edx
    subl 8(%ebp),%edx
    leal (%eax,%eax,2),%eax
    leal residents(,%eax,4),%eax
    leal (%eax,%edx,4),%edx
    pushl %edx
    call strcpy
    movl %ebp,%esp
    popl %ebp
    ret
```

A. What is the value of ROOMS?
B. Due to a strange bug, the program accesses residents [0] [1] [-2]. What value is actually being accessed? (Express your answer as residents [x][y][z] where $x, y$ and $z$ are all non-negative such that residents[x][y][z] access the same value. You may assume that FLOORS and ROOMS are both greater than 1)
C. The programmer realizes that this implementation is wasteful of memory. Successive fires in several memory chip factories in Taiwan drive up memory prices and finally convince him to improve the memory efficiency of his implementation to maintain the competitiveness of the family hotel.

The declaration of residents is changed to be a two dimensional array of pointers to character strings (names). The new code allocates memory for customer names only for those rooms that are actually reserved. Otherwise, residents[f][r] stores a NULL pointer. For simplicity, assume there is no storage overhead due to malloc.

The new declaration looks like this:

```
char *residents[FLOORS][ROOMS];
void
reserve_room(int floor, int room, char *custname)
{
    residents[floor][room] = malloc(LEN);
    strcpy(residents[floor][room], custname);
}
```

After a few months. The programmer goes back to review the memory savings of his improved scheme. During that period, the hotel was $20 \%$ reserved. The programmer is delighted because the savings are found to be 168 bytes! How many floors does this hotel have? (that is, what is the value of FLOORS?)

## Problem 4. (10 points):

Condider the following assembly code for a C for loop:

```
loop:
        pushl %ebp
        movl %esp,%ebp
        movl 0x8(%ebp),%edx
        movl %edx,%eax
        addl 0xc(%ebp),%eax
        leal 0xfffffffff(%eax),%ecx
        cmpl %ecx,%edx
        jae .L4
.L6 :
        movb (%edx),%al
        xorb (%ecx),%al
        movb %al, (%edx)
        xorb (%ecx),%al
        movb %al, (%ecx)
        xorb %al,(%edx)
        incl %edx
        decl %ecx
        cmpl %ecx,%edx
        jb .L6
.L4:
    movl %ebp,%esp
    popl %ebp
    ret
```

Based on the assembly code above, fill in the blanks below in its corresponding C source code. (Note: you may only use the symbolic variables $\mathrm{h}, \mathrm{t}$ and len in your expressions below - do not use register names.)

```
void loop(char *h, int len)
{
    char *t;
    for (
```

$\qquad$

``` ;
``` \(\qquad\)
``` h++, t--) \{
```

$\qquad$
$\qquad$
$\qquad$

```
    }
    return;
}
```


## Problem 5. (6 points):

This problem concerns the following, low-quality code:

```
void foo(int x)
{
    int a[3];
    char buf[4];
    a[0] = 0xF0F1F2F3;
    a[1] = x;
    gets(buf);
    printf("a[0] = 0x%x, a[1] = 0x%x, buf = %s\n", a[0], a[1], buf);
}
```

In a program containing this code, procedure $f \circ \circ$ has the following disassembled form on an IA32 machine:

```
080485d0 <foo>:
80485d0: 55
80485d1: 89 e5
80485d3: 83 ec 10
80485d6:
80485d7:
80485da:
80485df:
80485e1:
80485e4:
80485e7:
80485e8:
80485ed:
80485ee:
80485f1:
80485f2:
80485f5:
80485f6: 68 ec 90 04 08
80485fb: e8 94 fe ff ff
8048600:
8048603:
8048605:
8048606:
8048607:
53
8b 45 08
f1 f0
89 45
                                f8
8048607: c
```

```
movl %eax,0xffffffff8(%ebp)
```

movl %eax,0xffffffff8(%ebp)
leal 0xffffffff0(%ebp),%ebx
leal 0xffffffff0(%ebp),%ebx
pushl %ebx
pushl %ebx
call 80484a4 <_init+0x54> \# gets
call 80484a4 <_init+0x54> \# gets
pushl %ebx
pushl %ebx
movl 0xffffffff8(%ebp),%eax
movl 0xffffffff8(%ebp),%eax
pushl %eax
pushl %eax
movl 0xffffffff4(%ebp),%eax
movl 0xffffffff4(%ebp),%eax
pushl %eax
pushl %eax
pushl \$0x80490ec
pushl \$0x80490ec
call 8048494 <_init+0x44> \# printf
call 8048494 <_init+0x44> \# printf
movl 0xfffffffec(%ebp),%ebx
movl 0xfffffffec(%ebp),%ebx
movl %ebp,%esp
movl %ebp,%esp
popl %ebp
popl %ebp
ret
ret

```
pushl %ebp
```

pushl %ebp
movl %esp,%ebp
movl %esp,%ebp
subl \$0x10,%esp
subl \$0x10,%esp
pushl %ebx
pushl %ebx
movl 0x8(%ebp),%eax
movl 0x8(%ebp),%eax
movl \$0xf0f1f2f3,0xffffffff4(%ebp)
movl \$0xf0f1f2f3,0xffffffff4(%ebp)
nop

```
nop
```

For the following questions, recall that:

- gets is a standard C library routine.
- IA32 machines are little-endian.
- C strings are null-terminated (i.e., terminated by a character with value $0 x 00$ ).
- Characters ' 0 ' through ' 9 ' have ASCII codes $0 \times 30$ through $0 \times 39$.

Fill in the following table indicating where on the stack the following program values are located. Express these as decimal offsets (positive or negative) relative to register \%ebp:

| Program Value | Decimal Offset |
| :--- | :--- |
| $a$ |  |
| $a[2]$ |  |
| $x$ |  |
| buf |  |
| buf [3] |  |
| Saved value of register \%ebx |  |

## Problem 6. (9 points):

The following problem concerns optimizing a procedure for maximum performance on an Intel Pentium III. Recall the following performance characteristics of the functional units for this machine:

| Operation | Latency | Issue Time |
| :--- | ---: | ---: |
| Integer Add | 1 | 1 |
| Integer Multiply | 4 | 1 |
| Integer Divide | 36 | 36 |
| Floating Point Add | 3 | 1 |
| Floating Point Multiply | 5 | 2 |
| Floating Point Divide | 38 | 38 |
| Load or Store (Cache Hit) | 1 | 1 |

Consider the following two procedures:

| Loop 1 | Loop 2 |
| :---: | :---: |
| ```int loop1(int *a, int x, int n) { int y = x*x; int i; for (i = 0; i < n; i++) x = y * a[i]; return x*y;``` | ```int loop2(int *a, int x, int n) { int y = x*x; int i; for (i = 0; i < n; i++) x = x * a[i]; return x*y;``` |
| \} | \} |

When compiled with GCC, we obtain the following assembly code for the inner loop:

| Loop 1 | Loop 2 |
| :--- | :--- |
| . L21: | .L27: |
| movl \%ecx, \%eax | imull (\%esi, \%edx, 4), \%eax |
| imull (\%esi, \%edx, 4), \%eax | incl \%edx |
| incl \%edx | cmpl \%ebx, \%edx |
| cmpl \%ebx, \%edx | jl .L27 |
| jl .L21 |  |

Running on a Intel Pentium III machine, we find that Loop 1 requires 3.0 clock cycles per iteration, while Loop 2 requires 4.0.
A. Explain how it is that Loop 1 is faster than Loop 2, even though it has one more instruction
B. By using the compiler flag -funroll-loops, we can compile the code to use 4-way loop unrolling. This speeds up Loop 1. Explain why.
C. Even with loop unrolling, we find the performance of Loop 2 remains the same. Explain why.

## Problem 7. (5 points):

The following problem concerns basic cache lookups.

- The memory is byte addressable.
- Memory accesses are to 1-byte words (not 4-byte words).
- Physical addresses are 13 bits wide.
- The cache is 2 -way set associative, with a 4 byte line size and 16 total lines.

In the following tables, all numbers are given in hexadecimal. The contents of the cache are as follows:

| 2-way Set Associative Cache |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Index | Tag | Valid | Byte 0 | Byte 1 | Byte 2 | Byte 3 | Tag | Valid | Byte 0 | Byte 1 | Byte 2 | Byte 3 |
| 0 | 09 | 1 | 86 | 30 | 3F | 10 | 00 | 0 | 99 | 04 | 03 | 48 |
| 1 | 45 | 1 | 60 | 4F | E0 | 23 | 38 | 1 | 00 | BC | 0B | 37 |
| 2 | EB | 0 | 2F | 81 | FD | 09 | 0B | 0 | 8 F | E2 | 05 | BD |
| 3 | 06 | 0 | 3D | 94 | 9 B | F7 | 32 | 1 | 12 | 08 | 7B | AD |
| 4 | C7 | 1 | 06 | 78 | 07 | C5 | 05 | 1 | 40 | 67 | C2 | 3B |
| 5 | 71 | 1 | 0B | DE | 18 | 4B | 6 E | 0 | B0 | 39 | D3 | F7 |
| 6 | 91 | 1 | A0 | B7 | 26 | 2D | F0 | 0 | 0C | 71 | 40 | 10 |
| 7 | 46 | 0 | B1 | 0A | 32 | 0F | DE | 1 | 12 | C0 | 88 | 37 |

## Part 1

The box below shows the format of a physical address. Indicate (by labeling the diagram) the fields that would be used to determine the following:
$C O$ The block offset within the cache line
CI The cache index
$C T$ The cache tag

| 12 | 11 | 10 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 | 0 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |  |  |  |  |  |

## Part 2

For the given physical address, indicate the cache entry accessed and the cache byte value returned in hex. Indicate whether a cache miss occurs.

If there is a cache miss, enter "-" for "Cache Byte returned".
Physical address: 0E34
A. Physical address format (one bit per box)

B. Physical memory reference

| Parameter | Value |
| :--- | :---: |
| Byte offset | 0 x |
| Cache Index | 0 x |
| Cache Tag | 0 x |
| Cache Hit? (Y/N) |  |
| Cache Byte returned | 0 x |

