## Datorarkitektur, 2009

## Tentamen 2009-03-13

## Instructions:

- Make sure that your exam is not missing any sheets, then write your full name on the front.
- Write your answers in the space provided below the problem. If you make a mess, clearly indicate your final answer.
- The exam has a maximum score of 60 points plus 3 possible bonus points.
- The aproximate limits for grades on this exam are:
- To pass (grade E): 30 points.
- For grade D: 37 points.
- For grade C: 45 points.
- For grade B: 52 points.
- For grade A: 59 points.
- The problems are of varying difficulty. The point value of each problem is indicated. Pile up the easy points quickly and then come back to the harder problems.
- This exam is OPEN BOOK. You may use any books or notes you like but no computer, calulator, telephone etc. Good luck!


## Problem 1. (9 points):

Assume we are running code on a 10-bit machine using two's complement arithmetic for signed integers. A "short" integer is encoded using 5 bits. Fill in the empty boxes in the table below. The following definitions are used in the table:

```
short sy = -6;
int y = sy;
int x = -23;
unsigned ux = x;
```

Note: You need not fill in entries marked with "-".

| Expression | Decimal Representation | Binary Representation |
| :---: | :---: | :---: |
| Zero | 0 |  |
| - | -10 |  |
| - | 29 | $011010 \quad 0010$ |
| - |  |  |
| $u x$ |  |  |
| $y$ |  |  |
| $x \gg 3$ |  |  |
| TMax |  |  |
| - TMin |  |  |
| TMax + TMax |  |  |
| TMin + TMin |  |  |

## Problem 2. (14 points):

Consider the following 12-bit floating point representation based on the IEEE floating point format:

- There is a sign bit in the most significant bit.
- The next five bits are the exponent. The exponent bias is 15 .
- The last six bits are the significand.

The rules are like those in the IEEE standard (normalized, denormalized, representation of 0 , infinity, and NAN).
We consider the floating point format to encode numbers in a form:

$$
(-1)^{s} \times m \times 2^{E}
$$

where $m$ is the mantissa and $E$ is the exponent.
Fill in the table below for the following numbers, with the following instructions for each column:
Hex: The 3 hexadecimal digits describing the encoded form.
$m$ : The fractional value of the mantissa. This should be a number of the form $x$ or $x / y$, where $x$ is an integer, and $y$ is an integral power of 2 . Examples include: $0,23 / 16$, and $1 / 64$.
$E$ : The integer value of the exponent.
Value: The numeric value represented. Use the notation $x$ or $x \times 2^{z}$, where $x$ and $z$ are integers.
As an example, to represent the number $7 / 2$, we would have $s=0, m=7 / 4$, and $E=1$. Our number would therefore have an exponent field of $0 \times 10$ (decimal value $15+1=16$ ) and a significand field $0 \times 30$ (binary $110000_{2}$ ), giving a hex representation 430.
You need not fill in entries marked "-".

| Description | Hex | $m$ | $E$ | Value |
| :--- | :---: | :---: | :---: | :---: |
| -0 |  |  |  | -0 |
| Smallest value $>1$ |  |  |  |  |
| 256 |  |  |  | - |
| Largest Denormalized |  |  |  |  |
| $-\infty$ |  | - | - | $-\infty$ |
| Number with hex representation 3A0 | 3A0 |  |  |  |

## Problem 3. (8 points):

Consider the source code below, where M and N are constants declared with \#define.

```
int mat1[M][N];
int mat2[N][M];
int copy_element(int i, int j)
{
    mat1[i][j] = mat2[j][i];
}
```

This generates the following assembly code:

```
copy_element:
    pushl %ebp
    movl %esp, %ebp
    movl 8(%ebp), %ecx
    leal (%ecx,%ecx,2), %edx
    sall $3, %edx
    movl 12(%ebp), %eax
    subl %ecx, %edx
    addl %eax, %edx
    leal (%eax,%eax,4), %eax
    addl %ecx, %eax
    movl mat2(,%eax,4), %eax
    movl %eax, mat1(,%edx,4)
    leave
    ret
```

A. What is the value of $M$ :
B. What is the value of N :

## Problem 4. (10 points):

## Buffer overflow

This problem concerns the following C code, excerpted from Dr. Evil's best-selling autobiography, "World Domination My Way". He calls the program NukeJr, his baby nuclear bomb phase.

```
/*
    * NukeJr - Dr. Evil's baby nuke
    */
#include <stdio.h>
#define EOF -1
int overflow(void);
int one = 1;
/* main - NukeJr's main routine */
int main() {
    int val = overflow();
    val += one;
    if (val != 15213)
        printf("Boom!\n");
    else
        printf("Curses! You've defused NukeJr!\n");
    _exit(0); /* syscall version of exit that doesn't need %ebp */
}
/* Overflow - writes to stack buffer and returns 15213 */
int overflow() {
    char buf[4];
    int val, i=0;
    while(scanf("%x", &val) != EOF)
        buf[i++] = (char)val;
    return 15213;
}
```


## Buffer overflow (cont)

Here is the corresponding machine code for NukeJr when compiled and linked on a Linux/x86 machine:

| 08048560 <main>: |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 8048560 : | 55 |  | pushl | \%ebp |  |
| 8048561: | 89 e5 |  | movl | \%esp, \%ebp |  |
| 8048563 : | 83 ec | 08 | subl | \$0x8, \%esp |  |
| 8048566 : | e8 31 | 000000 | call | 804859c <overflow> |  |
| 804856 b : | 0305 | $90 \quad 9604$ | addl | 0x8049690,\%eax | \# val += one; |
| 8048570 : | 08 |  |  |  |  |
| 8048571 : | 3d 6d | $3 b 00 \quad 00$ | cmpl | \$0x3b6d, \%eax | \# val == 15213? |
| 8048576 : | 74 0a |  | je | 8048582 <main+0x22> |  |
| 8048578 : | 83 c 4 | f4 | addl | \$0xfffffff 4 , |  |
| 804857 b : | 6840 | 860408 | pushl | \$0x8048640 |  |
| 8048580 : | eb 08 |  | jmp | 804858a <main+0x2a> |  |
| 8048582 : | 83 c4 | f 4 | addl | \$0xfffffff 4 , \%esp |  |
| 8048585 : | 6860 | 860408 | pushl | \$0x8048660 |  |
| 804858 a : | e8 75 | fe ff ff | call | 8048404 <_init+0x44> | \# call printf |
| 804858f: | 83 c 4 | 10 | addl | \$0x10, \%esp |  |
| 8048592 : | 83 c 4 | f4 | addl | \$0xfffffff 4 , \%esp |  |
| 0804859 c <overflow>: |  |  |  |  |  |
| 804859 c : | 55 |  | pushl | \%ebp |  |
| 804859 d : | 89 e5 |  | movl | \%esp, \%ebp |  |
| 804859 f : | 83 ec |  | subl | \$0x10, \%esp |  |
| 80485 a 2 : | 56 |  | pushl | \%esi |  |
| 80485a3: | 53 |  | pushl | \%ebx |  |
| 80485a4: | 31 f6 |  | xorl | \%esi, \%esi |  |
| 80485a6: | 8d 5d | f8 | leal | Oxfffffff (\%ebp) , \%ebx |  |
| 80485a9: | eb 0d |  | jmp | 80485 b 8 <overflow+0x1c |  |
| 80485 ab : | 90 |  | nop |  |  |
| 80485 ac : | 8d 74 | 2600 | leal | $0 x 0$ (\%esi, 1), \%esi |  |
| 80485 b 0 : | 8a 45 | f8 | movb | 0xfffffff8 (\%ebp), \%al | \# L1: loop start |
| 80485 b : | 8844 | 2 ffc | movb | \%al, Oxfffffffc (\%esi, \%e | bp, 1) |
| 80485 b 7 : | 46 |  | incl | \%esi |  |
| 80485 b : | 83 c 4 | f8 | addl | \$0xfffffff8, \%esp |  |
| 80485 bb : | 53 |  | pushl | \%ebx |  |
| 80485 bc : | 6880 | 860408 | pushl | \$0x8048680 |  |
| 80485c1: | e8 6e | fe ff ff | call | 8048434 <_init+0x74> | \# call scanf |
| 80485c6: | 83 c 4 | 10 | addl | \$0x10, \%esp |  |
| 80485 c 9 : | 83 f8 | ff | cmpl | \$0xffffffff, \%eax |  |
| 80485 cc : | 75 e2 |  | jne | 80485b0 <overflow+0x14 | > \# goto L1 |
| 80485 ce : | b8 6d | 3 b 0000 | movl | \$0x3b6d, \%eax |  |
| 80485d3: | 8d 65 |  | leal | Oxffffffe8 (\%ebp) , \%esp |  |
| 80485d6: | 5b |  | popl | \%ebx |  |
| $80485 d 7$ : | 5 e |  | popl | \%esi |  |
| $80485 \mathrm{d8}$ : | 89 ec |  | movl | \%ebp, \%esp |  |
| 80485 da : | 5d |  | popl | \%ebp |  |
| 80485 db : | c3 |  | ret |  |  |

## Buffer overflow (cont)

This problem tests your understanding of the stack discipline and byte ordering. Here are some notes to help you work the problem:

- Recall that Linux/x86 machines are Little Endian.
- The scanf("\%x", \&val) function reads a whitespace-delimited sequence of characters from stdin that represents a hex integer, converts the sequence to a 32 -bit int, and assigns the result to val. The call to scanf returns either 1 (if it converted a sequence) or EOF (if no more sequences on stdin).
For example, calling scanf four time on the input string "0 a ff" would have the following result:
- 1st call to scanf: val=0x0 and scanf returns 1 .
- 2nd call to scanf: val=0xa and scanf returns 1 .
- 3rd call to scanf: val=0xff and scanf returns 1 .
- 4th call to scanf: val=? and scanf returns EOF.


## Buffer overflow (questions):

A. After the subl instruction at address $0 \times 804859 \mathrm{f}$ in function overflow completes, the stack contains a number of objects which are shown in the table below. Determine the address of each object as a byte offset from buf [0].

| Stack object | Address of stack object |
| :---: | :---: |
| return address | \&buf[0] + |
| old \%ebp | \&buf [0] + |
| buf[3] | \&buf [0] + |
| buf[2] | \&buf [0] + |
| buf[1] | \&buf[0] + 1 |
| buf[0] | \&buf[0] + 0 |

B. What input string would defuse NukeJr by causing the call to overflow to return to address $0 \times 8048571$ instead of 804856 b? Notes: (i) Your solution is allowed to trash the contents of the \%ebp register. (ii) Each underscore is a one or two digit hex number.

```
Answer: "0 0 0 0
```


## Problem 5. (8 points):

In this problem you will specify how to implement some new instructions for the Y86 machine.
The actions of an instruction is decribed inte the coursebook by a table that shows what is done in each step of the machine. Here are three examples:

| Stage | OPl rA, rB | irmovl V, rB | pushl rA |
| :---: | :---: | :---: | :---: |
| Fetch | icode:ifun $\leftarrow \mathrm{M}_{1}[\mathrm{PC}]$ $\mathrm{rA}: \mathrm{rB} \leftarrow \mathrm{M}_{1}[\mathrm{PC}+1]$ $\mathrm{valP} \leftarrow \mathrm{PC}+2$ | icode:ifun $\leftarrow \mathrm{M}_{1}[\mathrm{PC}]$ $\begin{aligned} & \mathrm{rA}: \mathrm{rB} \leftarrow \mathrm{M}_{1}[\mathrm{PC}+1] \\ & \mathrm{valC} \leftarrow \mathrm{M}_{4}[\mathrm{PC}+2] \\ & \mathrm{valP} \leftarrow \mathrm{PC}+6 \end{aligned}$ | icode:ifun $\leftarrow \mathrm{M}_{1}[\mathrm{PC}]$ $\mathrm{rA}: \mathrm{rB} \leftarrow \mathrm{M}_{1}[\mathrm{PC}+1]$ $\mathrm{valP} \leftarrow \mathrm{PC}+2$ |
| Decode | $\begin{aligned} \mathrm{valA} & \leftarrow \mathrm{R}[\mathrm{rA}] \\ \mathrm{valB} & \leftarrow \mathrm{R}[\mathrm{rB}] \end{aligned}$ |  | $\begin{aligned} \mathrm{valA} & \leftarrow \mathrm{R}[\mathrm{rA}] \\ \mathrm{valB} & \leftarrow \mathrm{R}[\% \mathrm{esp}] \end{aligned}$ |
| Execute | valE $\leftarrow$ valB OP valA <br> Set CC | valE $\leftarrow 0+$ valC | valE $\leftarrow \mathrm{valB}+(-4)$ |
| Memory |  |  | $\mathrm{M}_{4}[\mathrm{valE}] \leftarrow \mathrm{valA}$ |
| Write back | $\mathrm{R}[\mathrm{rB}] \leftarrow \mathrm{valE}$ | $\mathrm{R}[\mathrm{rB}] \leftarrow \mathrm{valE}$ | $\mathrm{R}[\% \mathrm{esp}] \leftarrow \mathrm{valE}$ |
| PC update | $\mathrm{PC} \leftarrow \mathrm{valP}$ | $\mathrm{PC} \leftarrow \mathrm{valP}$ | $\mathrm{PC} \leftarrow \mathrm{valP}$ |

You shall describe the three instructions incr, decr and not, that implements the following C-operations:

| instruction | C-operation |
| :--- | :--- |
| incr x | $\mathrm{x}=\mathrm{x}+1$ |
| $\operatorname{decr} \mathrm{x}$ | $\mathrm{x}=\mathrm{x}-1$ |
| not x | $\mathrm{x}=\sim \mathrm{x}$ |

All three instructions have the format:

| icode | ifun | 8 | rB |
| :--- | :--- | :--- | :--- |

All three instructions set the condition codes similar to OPl .

Fill in the operations done in each stage:

| Stage | incr rB | decr rB | not rB |
| :---: | :--- | :--- | :--- |
| Fetch | icode:ifun $\leftarrow \mathrm{M}_{1}[\mathrm{PC}]$ | icode:ifun $\leftarrow \mathrm{M}_{1}[\mathrm{PC}]$ | icode:ifun $\leftarrow \mathrm{M}_{1}[\mathrm{PC}]$ |
|  |  |  |  |
| Decode |  |  |  |
| Execute |  |  |  |
| PC update |  |  |  |
| Wemory |  |  |  |

## Problem 6. (8 points):

You are writing a new 3D game that you hope will earn you fame and fortune. You are currently working on a function to blank the screen buffer before drawing the next frame. The screen you are working with is a $640 \times 480$ array of pixels. The machine you are working on has a 64 KB direct mapped cache with 4 byte lines. The C structures you are using are:

```
struct pixel {
    char r;
    char g;
    char b;
    char a;
};
struct pixel buffer[480][640];
register int i, j;
register char *cptr;
register int *iptr;
```

Assume:

- sizeof(char) = 1
- sizeof(int) = 4
- buffer begins at memory address 0
- The cache is initially empty.
- The only memory accesses are to the entries of the array buffer. Variables $i, j$, cptr, and iptr are stored in registers.
A. What percentage of the writes in the following code will miss in the cache?

```
for (j=0; j < 640; j++) {
    for (i=0; i < 480; i++){
        buffer[i][j].r = 0;
        buffer[i][j].g = 0;
        buffer[i][j].b = 0;
        buffer[i][j].a = 0;
    }
}
```

Miss rate for writes to buffer: $\qquad$ \%
B. What percentage of the writes in the following code will miss in the cache?

```
char * cptr;
cptr = (char *) buffer;
for (; cptr < (((char *) buffer) + 640 * 480 * 4); cptr++)
    *cptr = 0;
```

Miss rate for writes to buffer: $\qquad$ \%
C. What percentage of the writes in the following code will miss in the cache?

```
int *iptr;
iptr = (int *) buffer;
for (; iptr < (buffer + 640 * 480); iptr++)
    *iptr = 0;
```

Miss rate for writes to buffer: $\qquad$ $\%$
D. Which code (A, B, or C) should be the fastest? $\qquad$

## Problem 7. (3 points):

Consider the following C functions and assembly code:

```
int fun1(int a, int b)
{
    unsigned ua = (unsigned) a;
    if (ua < b)
        return b;
    else
        return ua;
} funX:
int fun2(int a, int b)
{
    if (b < a)
        return b;
    else
        return a;
}
int fun3(int a, int b)
{
    if (a < b)
        return a;
    else
        return b;
}
```

Which of the functions compiled into the assembly code shown?

