

# Summary

# Concept Learning

- Hypotheses Space
- Relations between hypotheses
- Version Space
- Find-S
- Candidate Elimination
- Bias
- Bias-Variance Tradeoff
- Occam's Razor
- Generalization

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  - Bias
    - Bias of the Learner
    - Bias of the Data
  - Generalization

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- **Candidate Elimination**
- Bias
- Error Bound
- Complexity
- Generalization

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- **Bias**
  - Restriction Bias
  - Preference Bias
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- Entropy — unpredictability
- Information Gain
- Overfitting
  - Adaptation to non-generalizing details
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# Artificial Neuronal Networks

- Single Layer Networks
- Linear Separation
- Learning based on Error Minimization
- Multi Layer Networks
  - General Classification
  - Function Approximation
- Differentiable Threshold Functions
- Error Back-Propagation
- Convergence Properties

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# Bayesian Learning

- Maximum a'Posteriori (MAP)  
The most likely hypothesis given the observed data
- Maximum Likelihood (ML)  
The hypothesis with highest likelihood of generating the data we have
- Bayes Optimal Classifier

$$\operatorname{argmax}_v \sum_h P(v|h) \cdot P(h|D)$$

- Naive Bayes Classifier

$$\operatorname{argmax}_v P(v) \prod_i P(a_i|v)$$

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- Generate several classifiers
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- $k$ -Nearest Neighbor
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- Delayed Reward
- Temporal Credit Assignment
- Value Function
- Policy
- Temporal Difference techniques
- $Q$ -Learning
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# Learning Theory

- PAC-Learnable
- Probably ( $\delta$ ) Approximately ( $\epsilon$ ) Correct
- Complexity measured in  $\frac{1}{\delta}$ ,  $\frac{1}{\epsilon}$  och  $n$
- Number of Training Examples

$$m \geq \frac{1}{\epsilon} \left[ \ln |H| + \ln \frac{1}{\delta} \right]$$

- VC-dimension

$$\text{VC}(H) \leq \log_2 |H| \quad m \geq \frac{1}{\epsilon} \left[ 4 \log_2 \frac{2}{\delta} + 8 \text{VC}(H) \cdot \log_2 \frac{13}{\epsilon} \right]$$

- Errors During Learning

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- Sequential Covering
- Successive Specialization
- Greedy or Beam-search  
Heuristic Search
- Inverse Resolution  
Bottom-up: explain the examples

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- Support-Vector Machines  
Minimizing the VC-dimension  $\Rightarrow$  Optimal Generalization
- Learning of sequences/time-series  
Hidden Markov Models  
Kalman Filters
- Unsupervised Learning  
Self Organizing Maps
- Recurrent Neural Networks
- Hybrid Methods

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