

# Secure Information Flow as a Safety Problem

# Overview

- Introduction to secure information flow
- Type-Based approach
- Self composition
- Downgrading
- Self composition with downgrading
- Type directed transformation
- Conclusion

# Introduction

The termination insensitive secure information flow problem (non-interference) can be reduced to solving a safety problem via a simple program transformation.

The transformation is called Self-composition.

This paper generalizes this self-compositional approach with a form of information downgrading.

The authors combine this with a type-based approach to achieve a better way to analyse software.

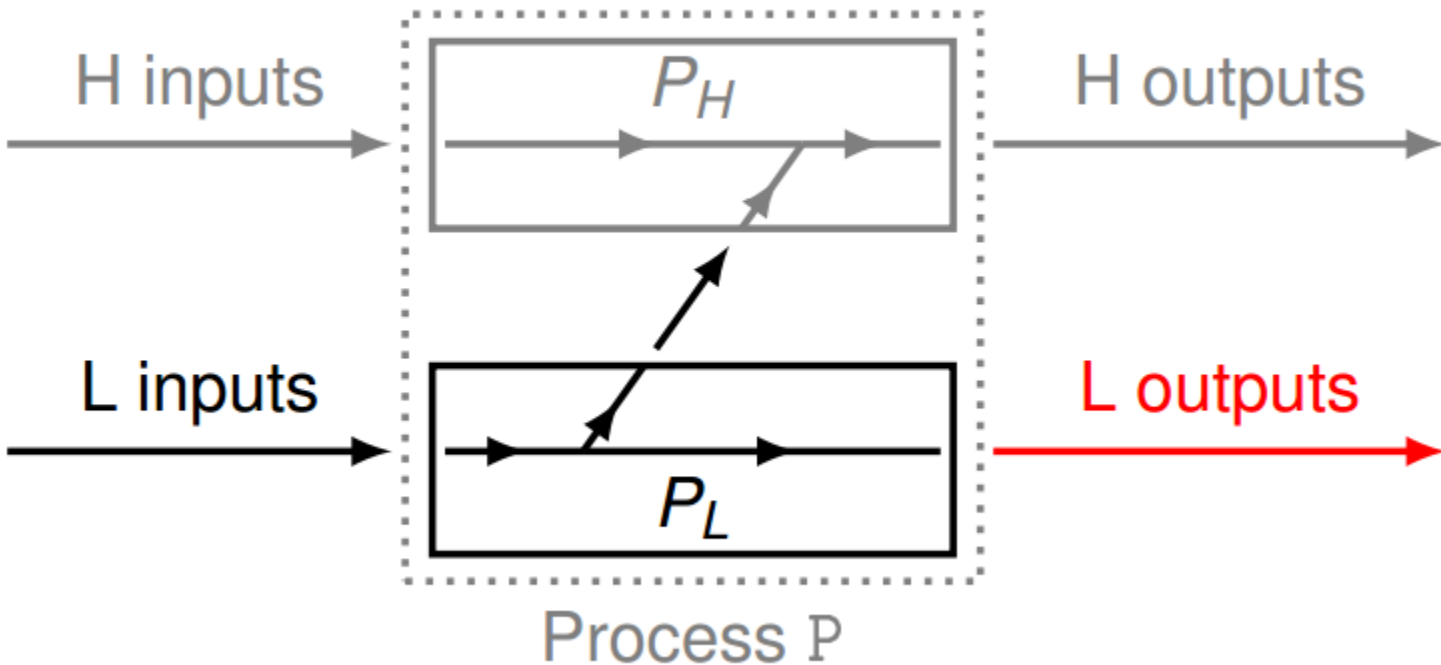
# Secure Information Flow

## Definition

*Given a program  $P$  whose variables  $H = \{h_1, \dots, h_n\}$  are high security variables and  $L = \{l_1, \dots, l_n\}$  are low-security variables,  $P$  is said to be secure if and only if for any stores  $M_1$  and  $M_2$  such that  $M_1 =_{Hc} M_2$ ,*

$$(\langle M_1, P \rangle \neq \perp \wedge \langle M_2, P \rangle \neq \perp) \Rightarrow \langle M_1, P \rangle =_L \langle M_2, P \rangle$$

# Non-Interference (Vanilla)



# Safety Problem

A safety property is a property of a program that can be refuted by observing a finite path

Non-interference is almost a safety problem

The 2-safety property is defined similarly but the program can be refuted by observing two finite paths

# Type-Based approach

Evaluates statically if the low security variables is dependent of the high security variables.

*if(b) then x:=1 else skip*  
*l:=l+x; **SAFE***

*if(h) then x:=1 else skip*  
*l:=l+x; **UNSAFE***

# Type-based limitation

Type-based cannot show that the example is safe

```
z := 1;  
if (h) then x := 1 else skip;  
if ( $\neg$ h) then x := z else skip;  
l := x + y
```



# Self-Composition

Type Based can't verify the previous figure, that's why we use Self-Composition because?

1. let  $V(P)$  be all variables in  $P$
2.  $C(P)$  is a copy of  $P$  where  $x \in V(P)$  is replaced by  $C(x)$
3. For any stores  $M_1$  and  $M_2$  such that  $\text{domain}(M_1) = V(P)$  and  $\text{domain}(M_2) = V(C(P))$ , let  $M_1 =_L M_2$  before execution
4. Run  $P;C(P)$
5. Check if  $\langle M_1, P;C(P) \rangle =_L \langle M_2, P;C(P) \rangle$

# Self-Composition

$z := 1;$

if ( $h$ ) then  $x := 1$  else skip;

if ( $\neg h$ ) then  $x := z$  else skip;

$l := x + y;$

$z' := 1;$

if ( $h'$ ) then  $x' := 1$  else skip;

if ( $\neg h'$ ) then  $x' := z'$  else skip

$l' := x' + y'$

# Downgrading 1

Vanilla secure information flow is too strict.  
For example:

```
if(hashfunc(input)=hash)  
    then  
        l:=secret  
    else  
        skip;
```

# Downgrading 2

In order to ease on the restrictions, we need a downgrading function  $f_{h_i}$  for each high security variable  $h_i$  that defines when and how a high security variable can be leaked.

Example (same as last page):

$f = \lambda x. \text{if}(\text{hashfunc}(\text{input})=\text{hash}) \text{ then } x \text{ else } c$

More examples:

$f = \lambda x. \text{length}(x)$

$f = \lambda x. 0$  (Vanilla)

# Downgrading 3

A program  $F$  can be expressed as  $F(f(h_1) \dots f(h_n)) = F(e_1 \dots e_n)$  and agree with  $P$  on low-security variables at termination.

where  $e_i$  is a security policy, that associates each high-security variable  $h_i$  to a downgrading function  $f_h$

The program  $F$  first evaluates the downgrading functions  $f(h_1) \dots f(h_n)$  so the  $(h_1, \dots, h_n)$  are not mentioned in the running of the rest of the program.

At termination  $\langle M, P \rangle =_L \langle M, F(e) \rangle$

# Downgrading and self composition

```
if (hashfunc(input) = hash) then  
    t := t + 1; l := l + secret  
else skip
```

Above does not work with type based

But it works with self composition

Because type based is dependent on structure of downgrading operations

# Self-Composition Problem

```
while ( $n > 0$ ) do
   $f_1 := f_1 + f_2$ ;  $f_2 := f_1 - f_2$ ;  $n := n - 1$ ;
if ( $f_1 > k$ ) then  $l := 1$  else  $l := 0$ ;
```

```
while ( $n > 0$ ) do
   $f_1 := f_1 + f_2$ ;  $f_2 := f_1 - f_2$ ;  $n := n - 1$ ;
if ( $f_1 > k$ ) then  $l := 1$  else  $l := 0$ ;
while ( $n' > 0$ ) do
   $f'_1 := f'_1 + f'_2$ ;  $f'_2 := f'_1 - f'_2$ ;  $n' := n' - 1$ ;
if ( $f'_1 > k'$ ) then  $l' := 1$  else  $l' := 0$ ;
```

Can't be verified with self-composition, but works with type-based.

# Type-directed Transformation

Both the type-based and the self-composition approach have their downsides.

Type-directed transformation combines the best of two worlds.

Using the WHILE-language to illustrate how it works.



# While-language

$P ::= x := e \mid \text{if } e \text{ then } P_1 \text{ else } P_2 \mid \text{while } e \text{ do } P \mid P_1; P_2 \mid \text{skip}$

$\varepsilon ::= [] \mid x := \varepsilon \mid \text{if } \varepsilon \text{ then } P_1 \text{ else } P_2 \mid \text{if } e \text{ then } \varepsilon \text{ else } P \mid \text{if } e \text{ then } P \text{ else } \varepsilon \mid$   
 $\text{while } \varepsilon \text{ do } P \mid \text{while } e \text{ do } \varepsilon \mid \varepsilon; P \mid P; \varepsilon$

# Type-directed translation

$$\frac{\Gamma \vdash e : \tau \text{ where } \tau \text{ is a low-security type}}{x := e \rightarrow_{\Gamma} x := e; C(x) := x}$$

$$\frac{\Gamma \not\vdash e : \tau \text{ where } \tau \text{ is a low-security type}}{x := e \rightarrow_{\Gamma} x := e; C(x) := C(e)}$$

$$\frac{\Gamma \vdash e : \tau \text{ where } \tau \text{ is a low-security type} \quad P_1 \rightarrow_{\Gamma} P_1^* \quad P_2 \rightarrow_{\Gamma} P_2^*}{\text{if } e \text{ then } P_1 \text{ else } P_2 \rightarrow_{\Gamma} \text{if } e \text{ then } P_1^* \text{ else } P_2^*}$$

$$\frac{\Gamma \not\vdash e : \tau \text{ where } \tau \text{ is a low-security type}}{\text{if } e \text{ then } P_1 \text{ else } P_2 \rightarrow_{\Gamma} \text{if } e \text{ then } P_1 \text{ else } P_2; \text{if } C(e) \text{ then } C(P_1) \text{ else } C(P_2)}$$

$$\frac{\Gamma \vdash e : \tau \text{ where } \tau \text{ is a low-security type} \quad P \rightarrow_{\Gamma} P^*}{\text{while } e \text{ do } s \rightarrow_{\Gamma} \text{while } e \text{ do } P^*}$$

$$\frac{\Gamma \not\vdash e : \tau \text{ where } \tau \text{ is a low-security type}}{\text{while } e \text{ do } P \rightarrow_{\Gamma} \text{while } e \text{ do } P; \text{while } C(e) \text{ do } C(P)}$$

$$\frac{P_1 \rightarrow_{\Gamma} P_1^* \quad P_2 \rightarrow_{\Gamma} P_2^*}{P_1; P_2 \rightarrow_{\Gamma} P_1^*; P_2^*} \quad \frac{}{\text{skip} \rightarrow_{\Gamma} \text{skip}}$$

# Type-directed translation

## Example 1

Before:  $\text{while } (n > 0) \text{ do}$   
 $f_1 := f_1 + f_2; f_2 := f_1 - f_2; n := n - 1;$   
 $\text{if } (h) \text{ then } x := 1 \text{ else skip;}$   
 $\text{if } (\neg h) \text{ then } x := 1 \text{ else skip;}$   
 $\text{while } (i < f_1) \text{ do}$   
 $l := l + x; i := i + 1$

Rule: 
$$\frac{\Gamma \vdash e : \tau \text{ where } \tau \text{ is a low-security type}}{x := e \rightarrow_{\Gamma} x := e; C(x) := x}$$

After:  $\text{while } (n > 0) \text{ do}$   
 $f_1 := f_1 + f_2; f'_1 := f_1; f_2 := f_1 - f_2; f'_2 := f_2;$   
 $n := n - 1; n' := n;$   
 $\text{if } (h) \text{ then } x := 1 \text{ else skip; if } (h') \text{ then } x' := 1 \text{ else skip;}$   
 $\text{if } (\neg h) \text{ then } x := 1 \text{ else skip; if } (\neg h') \text{ then } x' := 1 \text{ else skip;}$   
 $\text{while } (i < f_1) \text{ do}$   
 $l := l + x; l' := l' + x'; i := i + 1; i' := i$

# Type-directed translation

## Example 2

Before: 
$$\begin{array}{l} \text{while } (n > 0) \text{ do} \\ \quad f_1 := f_1 + f_2; f_2 := f_1 - f_2; n := n - 1; \\ \quad \text{if } (h) \text{ then } x := 1 \text{ else skip;} \\ \quad \text{if } (\neg h) \text{ then } x := 1 \text{ else skip;} \\ \quad \text{while } (i < f_1) \text{ do} \\ \quad \quad l := l + x; i := i + 1 \end{array}$$

Rule: 
$$\frac{\Gamma \not\vdash e : \tau \text{ where } \tau \text{ is a low-security type}}{\text{if } e \text{ then } P_1 \text{ else } P_2 \rightarrow_{\Gamma} \text{if } e \text{ then } P_1 \text{ else } P_2; \text{if } C(e) \text{ then } C(P_1) \text{ else } C(P_2)}$$

After: 
$$\begin{array}{l} \text{while } (n > 0) \text{ do} \\ \quad f_1 := f_1 + f_2; f'_1 := f_1; f_2 := f_1 - f_2; f'_2 := f_2; \\ \quad n := n - 1; n' := n; \\ \quad \text{if } (h) \text{ then } x := 1 \text{ else skip; if } (h') \text{ then } x' := 1 \text{ else skip;} \\ \quad \text{if } (\neg h) \text{ then } x := 1 \text{ else skip; if } (\neg h') \text{ then } x' := 1 \text{ else skip;} \\ \quad \text{while } (i < f_1) \text{ do} \\ \quad \quad l := l + x; l' := l' + x'; i := i + 1; i' := i \end{array}$$

# Type-directed translation

## Example 3

Before:  $\text{while } (n > 0) \text{ do}$   
     $f_1 := f_1 + f_2; f_2 := f_1 - f_2; n := n - 1;$   
    if  $(h)$  then  $x := 1$  else skip;  
    if  $(\neg h)$  then  $x := 1$  else skip;  
     $\text{while } (i < f_1) \text{ do}$   
         $l := l + x; i := i + 1$

Rule:  $\frac{\Gamma \vdash e : \tau \text{ where } \tau \text{ is a low-security type} \quad P \rightarrow_{\Gamma} P^*}{\text{while } e \text{ do } s \rightarrow_{\Gamma} \text{while } e \text{ do } P^*}$

After:  $\text{while } (n > 0) \text{ do}$   
     $f_1 := f_1 + f_2; f'_1 := f_1; f_2 := f_1 - f_2; f'_2 := f_2;$   
     $n := n - 1; n' := n;$   
    if  $(h)$  then  $x := 1$  else skip; if  $(h')$  then  $x' := 1$  else skip;  
    if  $(\neg h)$  then  $x := 1$  else skip; if  $(\neg h')$  then  $x' := 1$  else skip;  
     $\text{while } (i < f_1) \text{ do}$   
         $l := l + x; l' := l' + x'; i := i + 1; i' := i$

# Conclusion

- Type-directed transformation is better than the type based approach.
- But not much different to self-composed approach for a hypothetical analysis tool
- More digestible than self-composed
- Still not perfect.