# Mathematical Models, Analysis and Simulation Part I, Fall 2009

August 21, 2009

## Homework 2, Strang Ch. 1. Max. score 3.0, Deadline Sun Sep. 13

#### 1. **(2.3)**

**1.6:**15,19(p75ff);**1.7:**2,10,11,12(p88);

from G.Strang, Intro. to Applied Mathematics: 1.6:2,20,29 (pages copied and handed out)

#### 2. **(0.5)**

This is a modified version of P6.3.4 in Charles van Loan: Introduction to Scientific Computing. A and C are given n-by-n matrices, A is nonsingular. g and h are given n-vectors. Develop different algorithms (at least three) for computing n-vectors y and z so that

$$A^T y + Cz = g, Az = h$$

Implement them in Matlab and measure their run-times. Explain your observations. Choose test matrices of different sizes (say, n = 500, 1000, 1500, 2000) and measure the execution time. The following code snippet gives a hint:

```
tstart = cputime;
% insert your code to be timed
tend = cputime;
duration = tend-tstart;
```

A random square matrix can be generated by rand which gives (pseudo-) random numbers uniformly distributed in [0,1]:

```
n = 100;
A = 2*eye(n)+rand(n);
C = rand(n);
```

Note

Is A sure to be non-singular? No, but the probability of finding a singular one is zero. You may find it amusing to plot the spectrum of a large number of A's - use lam = eig(A); plot(lam,'.'); hold on;

### 3. **(0.2)**

The game changes when C is non-singular,  $n \times n$ , but A is  $m \times n, m < n$ . Then h is an m-vector as is y. Why not m > n? Eliminate y and show that the resulting system for z has coefficient matrix  $AC^{-1}A^T$  - called the Schur complement.