

5

Discrete system of equations:

$$U \in V_h \Rightarrow U = \sum_{j=1}^M \alpha_j \phi_j, \quad \alpha_j = U(N_j)$$

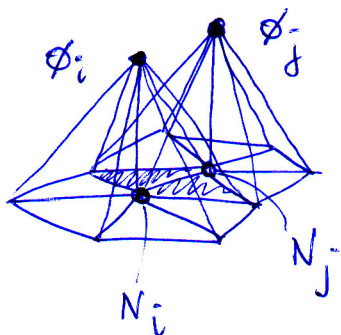
(6) & choosing $v = \phi_i \Rightarrow$

$$\sum_{j=1}^M (\nabla \phi_j, \nabla \phi_i) \alpha_j = (f, \phi_i) \quad i=1, \dots, M$$

Which is the same as $A \alpha = b$

$$A = (a_{ij}); \quad a_{ij} = (\nabla \phi_j, \nabla \phi_i) \quad (\text{stiffness matrix})$$

$$b = (b_i); \quad b_i = (f, \phi_i) \quad (\text{load vector})$$



a_{ij} non-zero only if

ϕ_i and ϕ_j have common

support: that is only if

$i=j$ or if N_i and N_j

are neighbors.

$$a_{ij} = \sum_k a_{ij}^k; \quad a_{ij}^k \text{ ~~stiffness matrix~~ stiffness matrix}$$

↑ contribution for element k

The sum is taken over the common support

of ϕ_i and ϕ_j : $\text{supp}(\phi_i) \cap \text{supp}(\phi_j)$