

**Preliminary weekly plan**

“sol.publ” = solution in “Hints & solutions...” on home page;

“hint.publ.” = hints in - “ -

The list of problems for each exercise is indicative. Not all problems will be worked; there will also be additions.

**Week 36**

Lecture 1 Mon 3 Sep 13-15 D34

*Introduction, function spaces, Poisson 1D, boundary conditions, weak formulation, Galerkin method, piecewise polynomials 1D* (CDE (1-4),5-6;8.1)

Lecture 2 Wed 5 Sep 8-10 D31

*Poisson 2D, FEM mesh, piecewise polynomials 2D*, (CDE 5.5;13;14.1-2,4;15.1)

Exercise 1 Fri 7 Sep 8-10 D31

*Variational form of DE, Galerkin method, boundary conditions, corresponding system of equations:*

Problems for Ex 1 and Ex 2:

4.21p73: sol. publ.;

6.2p108: matrix singular for some  $\lambda$ ;

8,9,10,11p119: sol. published; compute matrix & vector;

14p123: DE->Var;

8.6,7p183: sol.publ.; compute matrix & vector; 8.7- depends on c.;

9,10p184: sol.publ.; many other solutions possible, show some;

13.30p310: hint.publ.; Green I & II from Gauss.

15.14p356: DE  $\Leftrightarrow$  Var - cont. second derivatives of  $u$ ?;

16p357-trivial; 44p385-matrix/Robin cond.;

(4.22,24,25; 6.12)

**Week 37**

Lecture 3 Mon 10 Sep 13-15 D34

*Interpolation, piecewise polynomials, error estimation, adaptivity* (CDE 5,8,14,15)

Exercise 2 Tue 11 Sep 8-10 E32

Problems: see E1, and

21.a(.,.) & L: 1p513-hint.publ.,

Lecture 4 Wed 12 Sep 15-17 D31

*FEM algorithms and software; assembly, mapping, quadrature, implementation in Puffin* (CDE 14;15.1)

Exercise 3 Thu 13 Sep 15-17 E31

*Interpolation, error estimation:*

Problems:

5. poly.interp: 8p79-sol.publ.,trivial; 9p81-hint publ., cf. num.anal. book; 13,14p83-hint publ.;

17p84- notation in publ.sol.?

piecew.poly.:23p88-hint publ.; 24p90-trivial;

8.11p186-matrix again; 12p188-matrix w Robin cond.; 16p189-matrix w quadrature;

Error estimates: 17p190-sol.publ.; 18p191-sol.publ.; 20p193-sol.publ.; 21,23p194;

Beam eq'n: 37,40,41p203 - a big problem;

14.9p329-sol.publ. trivial;

Lab 1 Fri 14 Sep 8-10 4V4Gul, 4V6Bru

Project A

**Week 38**

Lecture 5      Mon 17 Sep    13-15   D34  
*IVP, Heat equation, Wave equation, Stability, theta-method, space-time FEM*  
(CDE 9,10,16,17)

Exercise 4      Wed 19 Sep    15-17   D31  
*Stability, IVP, etc.*

Problems:

**9.** ODEscalar.math: 4p207;5,7p208; cGal:11,14p212; dGal:15,16p214;43p234;  
**10.** ODEsyst.estimate: 18,21p257; 24(a)p259; 27,28p260; dGal:30p262;  
**16.** 14p405,15p406,cGdG:18p407;  
**17.** Wave energy: 19,20p434, radial: 21p435, energy: 27p438;  
(**9.**23,24,25,40,41,42; **16.**19,20; **17.**37(a))

Lecture 6      Thu 20 Sep    15-17   E53  
*Abstract problem, Lax-Milgram Theorem* (CDE 7,8,21)

Lab 2           Fri 21 Sep      8-10    4V2Rod, 4V3Ora  
Project A

**Week 39**

Lecture 7      Mon 24 Sep    13-15   D34  
*Adaptivity, error estimation, a priori, a posteriori, duality*

Exercise 5      Wed 26 Sep    15-17   D31  
*Abstract problem, Lax-Milgram Theorem; Error estimation, a priori, a posteriori, duality:*

Problems:

**8.**  $a$  &  $a^{-1}$ : 17p190;  
**9.** ODEestimate:10p210;  
**21.** LaxM: 9p520-sol.publ.,12,13p521-sol.publ.  
+ extra.

Lab 3           Thu 27 Sep    15-17   4V2Rod, 4V3Ora  
Project A

Deadline      Fri 28 Sep    17.00  
Report ProjA + HWA

**Week 40**

Lecture 8      Mon 1 Oct     13-15   E51  
*Space-time FEM, transport, Convection-Diffusion, stabilization* (CDE 18,19);  
Problem **18.6**

Exercise 6      Wed 3 Oct     15-17   Q26-07  
*Error estimation, a priori, a posteriori, duality, stabilization:*

Problems:

**18.** Convection: 1p453-trivial, 3,4p458(also  $\beta = (-x_2, x_1)$ ), Sd: 7p463, Sd stab.est.: 9p466;  
Green'sf.: 12p470;  
**19.** Characteristics: 1p479-trivial, Lagrange: 2p480,4p481

Lab 4           Thu 4 Oct     15-17   4V4Gul, 4V6Bru  
Project B

DN2260 Finite Elements Fall 07 Prel. Schedule p 3 (3)  
J.O. CSC KTH

**Week 41**

Lecture 9      Mon 8 Oct      13-15    D31  
*Navier-Stokes, adaptivity, overview/review*

Lab 5            Tue 9 Oct        15-17    4V2Rod, 4V3Ora  
Project B

Exercise 7      Wed 10 Oct      15-17    E32  
*Repetition, preparation for written exam.*  
Problems: Leftovers, extra problems, old exams

Lab 6            Thu 11 Oct      13-15    4V2Rod, 4V3Ora  
Project B

Deadline        Fri 19 Oct      17.00  
Report ProjB + HWB

**Week 42**

Written exam    Thu 25 Oct      14-19    M31. M32